Computerized Classification Testing in More Than Two Categories Using Stochastic Curtailment

Jasper T. Wouda
Theo J.H.M. Eggen
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Abstract

Computerized classification testing (CCT) can be used to increase efficiency in educational measurement. The truncated sequential probability ratio test (TSPRT) has been widely studied as a decision algorithm in CCT for 2 or more categories. Finkelman (2003) added an algorithm to the TSPRT in the form of stochastic curtailment to classify an examinee in an even earlier stage of testing. This stochastically curtailed SPRT (SCSPRT) halts testing when a change of classification is possible, but unlikely. Finkelman (2003) adapted the algorithm for 2 categories and with fixed item ordering. The present study replicated his results, then replicated them in realistic settings, and subsequently generalized the SCSPRT to 3 categories while using adaptive item selection. The results show increased efficiency when using 1 and 2 cut points. Different item selection methods are discussed.
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Computerized Classification Testing

Applications of computerized classification testing (CCT) show how adaptive testing can be used to increase efficiency in educational measurement. CCT differs from conventional computerized adaptive testing (CAT) in that in CCT, a person’s exact (latent) ability level, $\theta_i$, is not especially important as long as this person is correctly classified after reaching a certain threshold. Classifying a person can be important in determining whether someone has reached a certain level of proficiency in, for instance, mathematics. For both CCT and CAT, the item banks that are usually used have been calibrated using item response theory (IRT).

The SPRT is a widely used method for classification problems in CCT (see Thompson, 2007, for an overview of the different methods used). The SCSPRT (Finkelman, 2003, 2004, 2008) is an expansion of the SPRT, but as it is used now, it is only applicable for mastery testing (CCT with one cut point). This is because it needs information of $N$ items (the maximum number of items) minus $k$ items (the current number of items administered) to come to a classification decision. To obtain information about these ‘future’ items, using the SCSPRT as it is used now, a test is needed that uses fixed item ordering. Fixed item ordering has so far only been useful in classification problems that use one cut point.

The present study

In the present study, the SCSPRT was generalized to three classification levels or two cut points. Consequently, the item selection algorithm had to be an adaptive one and the items could not stay fixed in the test (Eggen & Straetmans, 2000). In other words, in order to be effective, the SCSPRT had to be adapted to make it work with three classification levels. After a brief explanation of the SPRT, the SCSPRT will be discussed. Subsequently, attention will be given to the modification of the SCSPRT for three classification levels. Then replications of the simulations conducted by Finkelman (2003) and testing the algorithm with realistic settings will be presented. This replication was carried out not only to test our implementation of the SCSPRT, but also because it was not an exact replication; in this study a slightly different version of the item information function was used, together with a different likelihood estimator.

The final step was to test the adapted SCSPRT with two cut points, using simulated data with real parameters, realistic ability ($\theta$-) distributions, and sensible cut points. The goal of this study was to test the SCSPRT in somewhat more realistic settings, generalize it to more than two classification levels, and determine which item selection method has the largest efficiency gain, while keeping usability in mind.

The IRT Model

Before discussing the SPRT, some of the basic IRT used in this study is introduced. Let $u_{ij}$ be 1 if a given respondent $i$ has answered item $j$ correctly, and 0 if the respondent has answered the item incorrectly. In item response theory (IRT), the $i^{th}$ student’s ability is regularly denoted as a latent variable $\theta_i$. Although $\theta$ is assumed to vary from person to person, the subscript $i$ is dropped at this point for simplicity. In this study, the IRT model
used is the two-parameter logistic (2PL) model, which is given by (Birnbaum, 1968) as

\[ p_j(\theta) = P(U_j = 1|\theta) = \frac{\exp a_j(\theta - b_j)}{1 + \exp a_j(\theta - b_j)} \]  

(1)

in which \(b_j\) is the difficulty parameter and \(a_j\) the discrimination parameter. The estimator of ability \(\theta\) used here to estimate the maximum likelihood of theta is the weighted maximum likelihood (WML) estimator, developed by Warm (1989). In the 2PL model, this WML estimator is given by

\[ \hat{\theta}(k) = \max_{\theta} \left( \sum_{j=1}^{k} I_j(\theta) \prod_{j=1}^{k} p_j(\theta)(1 - p_j(\theta)) \right) . \]  

(2)

This is the generally statistically superior variant of the unweighted maximum likelihood estimator (Eggen, 1999) in which \(k\) is the number of items and \(I_j(\theta)\) is the Fisher item information of item \(j\). In the 2PL model, this function is given by

\[ I_j(\theta) = a_j^2 p_j(\theta)(1 - p_j(\theta)). \]  

(3)

The Sequential Probability Ratio Test

The Sequential Probability Ratio Test (SPRT) is a widely used method in CCT for determining to which of a limited number of categories the classification level of an examinee belongs. The first applications of Wald’s (1947) SPRT in CCT (Lewis & Sheenan, 1990; Reckase, 1983; Spray & Reckase 1994, 1996) involved only one cut point on the latent scale with two categories (e.g., mastery and non-mastery). Eggen and Straetmans (2000) and Spray (1993) showed that the SPRT can also be utilized in a CCT for classification into one of three categories. Users of the SPRT procedure (e.g., Jiao, Wang, & Lau, 2004; Eggen & Straetmans, 2000) typically set a maximum to the number of items to be administered under real testing conditions. This is often implemented as an extra stopping rule at \(k = N\) items, where \(k\) is the number of currently administered items and \(N\) is the defined maximum number of items to be administered. This feature makes this procedure a truncated form of the conventional SPRT (TSPRT).

The Truncated Sequential Probability Ratio Test (TSPRT)

The TSPRT is a sequential testing procedure in which the likelihoods of a statistical hypothesis and an alternative are compared. First cut points have to be set on the proficiency scale to determine the classification levels. Subsequently, indifference regions \(\delta\) are assigned around these cut points (See Eggen & Straetmans, 2000). These indifference regions can be seen as the areas in which it is most difficult for the TSPRT to classify an examinee. Therefore the outer bounds of these regions are used for comparing the ratio test. The cut points plus or minus the indifference regions mark the two values for which the TSPRT compares the likelihoods. The basic TSPRT rationale is the evaluation of the ratio of two likelihoods. These values are then used to test two statistical hypotheses against one another. In the case of two cut points, \(\theta_1\) and \(\theta_2\), these hypotheses are (Eggen & Straetmans, 2000)
\[ H_{01} : \theta \leq \theta_1 - \delta_{11} \] (level 1) \[ H_{11} : \theta \geq \theta_1 + \delta_{12} \] (higher than 1) \[ H_{02} : \theta \leq \theta_2 - \delta_{12} \] (lower than 3) \[ H_{12} : \theta \geq \theta_2 + \delta_{22} \] (level 3).

Table I presents the ratio tests in the form of stopping rules of the TSPRT as used by Eggen and Straetmans (2000) and Jiao, Wang and Lau (2004). These are in fact generalizations of the stopping rules as used by Finkelman (2003, 2008) in the one cut point case. In Table 1, \( \alpha \) and \( \beta \) are constants representing the allowed decision error rates of the two statistical tests. The first stopping rule stops testing and accepts level one if the weighted sum score is smaller than or equal to the log of the constant (which depends on the error rates) minus the sum of the log likelihood ratios of the values at which the hypotheses are tested, divided by the sum of the \( \delta \)-values around that cut point. At \( k = N \), testing is stopped and a classification decision is forced. The decision rules at \( k = N \) are the ratio tests shown in Table I which are evaluated against the weighted sum. These decision rules are the same as the stopping rules, but without the \( \ln(\beta/(1 - \alpha)) \) or \( \ln((1 - \beta)/\alpha) \) parts.

| Table 1: Stopping rules of the Truncated Sequential Probability Ratio Test |
|-------------------------------|-------------------------------|
| If \( k < k^* < N \)            | If \( k < k^* < N \)            |
| Stop testing                  | Stop testing                  |
| and accept                    | and accept                    |
| level 1 if                     | level 2 if                     |
| \( \sum_{j=1}^{k} a_j u_j \leq \frac{\ln\left(\frac{\beta_1}{1-\alpha_1}\right) - \sum_{j=1}^{k} \ln\left(1 - p_j(\theta_1 + \delta_{12})/(1 - p_j(\theta_1 - \delta_{11}))\right)}{\delta_{11} + \delta_{12}} \) | \( \frac{\ln\left(1 - p_j(\theta_1 + \delta_{12})/(1 - p_j(\theta_1 - \delta_{11}))\right)}{\delta_{11} + \delta_{12}} \) \leq \( \sum_{j=1}^{k} a_j u_j \leq \frac{\ln\left(1 - p_j(\theta_2 + \delta_{22})/(1 - p_j(\theta_2 - \delta_{21}))\right)}{\delta_{21} + \delta_{22}} \) |
| Stop testing                  | Stop testing                  |
| and accept                    | and accept                    |
| level 3 if                     | level 3 if                     |
| \( \sum_{j=1}^{k} a_j u_j \geq \frac{\ln\left(1 - p_j(\theta_1 + \delta_{12})/(1 - p_j(\theta_1 - \delta_{11}))\right)}{\delta_{11} + \delta_{12}} \) | \( \sum_{j=1}^{k} a_j u_j \geq \frac{\ln\left(1 - p_j(\theta_2 + \delta_{22})/(1 - p_j(\theta_2 - \delta_{21}))\right)}{\delta_{21} + \delta_{22}} \) |
| else                           | else                           |
| continue testing              | continue testing              |

Figure 1 represents a flow chart of how the different classification decisions take place. This flow chart is applicable to the SPRT as well as the SCSPRT.

The SCSPRT

Finkelman (2004) states that the TSPRT is inefficient when there are cases in which it presents another item while this item cannot change the classification decision about the examinee. The SCSPRT intervenes in these cases and halts testing when a change in classification is impossible. This part is called curtailment. However, the SCSPRT also halts testing in cases in which the probability of a change of classification decision is smaller than a predefined value, which is called stochastic curtailment. Finkelman (2003, 2008) showed that the TSPRT can be stochastically curtailed in order to shorten test length, while gaining classification accuracy. Usually, in CAT, it is optimal to choose items which provide maximum information at the current ability estimate. Thus, the test is adapted to
the difficulty an examinee can handle. In mastery testing, it is optimal to choose items which have maximum information at the cut point (Eggen, 1999). This way the test only stays adaptive in test length, but stops being adaptive in the selection of items. The problem of CCT with three classification levels is that there are two cut points. With one cut point, it would have been clear around which cut point items have to be administered, because there is only one. With two cut points, there is no best choice. Around which cut point items will be most informative for an examinee differs for each examinee. This difference is explained by differences in ability between examinees. The other problem is that the SCSPRT, as applied by Finkelman (2003), is constructed in such a way that it needs information of all \((N - k)\) items to be administered to make a classification decision. In the next section an answer to those problems is formulated in order to make the SCSPRT work in the case of three classification levels.

**Extension.** As can be seen in Finkelman (2003, 2008), the SCSPRT is an extension of the SPRT. It adds stochastic curtailment in the form of two extra stopping rules per level. Stochastic curtailment ceases testing and rejects \(H_0\) if, given \(k\) observations, the probability that a decision \(D\) will accept \(H_0\), \(P_k(D = H_0)\), is not higher than a set value \(1 - \gamma\). Testing stops and accepts \(H_0\) if this probability is at least \(\gamma\). As mentioned before, the TSPRT and the SCSPRT as used in a two-category problem have a set maximum
number of items $N$ (e.g., Spray & Reckase, 1996; Eggen, 1999; Finkelman 2003, 2004, 2008). When using one cut point, one can easily set item selection to be maximally informative at the cut point $\theta_0$. An advantage of maintaining this selection criterion is that all items that will be administered are known. If $k$ is the current number of items, then the possible future items, $N - k$, are known. Consequently, it can also be estimated whether, given the expected value of the rest of the items, future items would change the current classification at $k$ items.

Future items. However, in the present study, the aim was to extend the SCSPRT to three classification levels. This means that there are two cut scores, so maximum information at the cut score cannot be used as a selection criterion (Eggen, 1999). The problem is how to provide the SCSPRT with information of future $(N - k)$ items. It is not possible to know at which cut point one has to start administering items. One solution is to calculate the optimal descending ordering of item information after every administered item and to plug that into the SCSPRT as information of 'future items'. Other solutions could be to select items with the highest information around the cut point nearest to the current ability estimate or to select items in the middle, exactly between the two cut points.

The SCSPRT for Three Proficiency Levels

The SCSPRT uses fewer items than the SPRT. This means that there is less information to make a classification decision and this could cause higher decision error rates. In order to prevent misclassification due to imprecise estimations of theta, $\hat{\theta}$, we set, following Finkelman (2003), a minimum number of $k^* < N$ items that have to be completed before the extra stopping rules of the SCSPRT can take effect. So, until $k^* < k$, only the stopping rules of the TSPRT apply (see Table 1). Let (Finkelman, 2003)

$$T = \sum_{j=1}^{N} a_j p_j(\theta_1), \quad (4)$$

and let

$$S_k = \sum_{j=1}^{N} a_j u_j. \quad (5)$$

Then the first additional stopping rule stops testing and accepts $H0$ if

$$T > S_k + \sum_{j=k+1}^{N} a_j. \quad (6)$$

This is the case in which the weighted sum of item scores that have the highest information around the first cut point exceed the weighted sum of item scores of the administered items, plus the maximum score on the items to be administered which have the highest information around the current theta estimate. If the administered items have a higher value for the weighted sum of item scores $\sum_{j=1}^{k} a_j u_j$ than the value of $T$, then the rule breaks off testing and accepts $H1$. This is the curtailment stopping rule. The second additional stopping
rule, denoted as $P_k(D = H0)$, breaks off testing and accepts $H0$ if

$$
\Phi \left( \frac{T - S_k - \sum_{j=k+1}^{N} a_j p_j(\hat{\theta})}{\sqrt{\sum_{j=k+1}^{N} a_j^2 p_j(\hat{\theta})(1 - p_j(\hat{\theta}))}} \right) \geq \gamma.
$$

(7)

If the normal approximation ($\Phi$) of the weighted sum of item scores that have the highest information around the first cut point, minus the expected value at $N$ items, given $k$ already administered items, divided by the standard error of that expected value, is larger than or equal to a set value of $\gamma$, then the SCSPRT stops testing and accepts $H0$. However, this must go together with $\hat{\theta} < \theta_1$. Equation (7) is the stochastic curtailment stopping rule. The estimation of theta, $\tilde{\theta}$, as used in Equation (7), is a somewhat more conservative estimator of $\theta_k$ than $\hat{\theta}$. Finkelman (2003) sets this theta estimation to be

$$
\tilde{\theta} = \hat{\theta} + \frac{1}{\sqrt{\sum_{j=1}^{k} I(\hat{\theta}, u_j)}}
$$

(8)

if the value of $\hat{\theta}$ is smaller than the respective cut point value, and

$$
\tilde{\theta} = \hat{\theta} - \frac{1}{\sqrt{\sum_{j=1}^{k} I(\hat{\theta}, u_j)}}
$$

(9)

if the value of $\hat{\theta}$ is larger than the respective cut point value. These $\tilde{\theta}$ are the endpoints of the respective lower (Eq. (8)) and upper (Eq. (9)) one-sided confidence intervals of a theta estimation. As can be seen in Equations (6) and (7), both additional stopping rules need

<table>
<thead>
<tr>
<th>Table 2: Stopping rules of the SCSPRT for three classification levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>If $k^* &lt; k &lt; N$</td>
</tr>
<tr>
<td>Stop testing and</td>
</tr>
<tr>
<td>accept level 1 if</td>
</tr>
<tr>
<td>$SPRT (see Table 1)$</td>
</tr>
<tr>
<td>or if $T_{\theta_1} &gt; S_k + \sum_{j=k+1}^{N} a_j$</td>
</tr>
<tr>
<td>or if $\theta &lt; \theta_1 &amp; P_k(D = H0_1) \geq \gamma$</td>
</tr>
<tr>
<td>Stop testing and</td>
</tr>
<tr>
<td>accept level 2 if</td>
</tr>
<tr>
<td>$SPRT (see Table 1)$</td>
</tr>
<tr>
<td>or if $T_{\theta_1} &lt; S_k$</td>
</tr>
<tr>
<td>or if $\theta_1 &lt; \hat{\theta} &amp; P_k(D = H0_1) \leq 1 - \gamma$</td>
</tr>
<tr>
<td>Stop testing and</td>
</tr>
<tr>
<td>accept level 3 if</td>
</tr>
<tr>
<td>$SPRT (see Table 1)$</td>
</tr>
<tr>
<td>or if $T_{\theta_2} &lt; S_k$</td>
</tr>
<tr>
<td>or if $\hat{\theta} &gt; \theta_2 &amp; P_k(D = H0_2) \leq 1 - \gamma$</td>
</tr>
<tr>
<td>else continue testing</td>
</tr>
</tbody>
</table>

*Level 2 is accepted only if one or more stopping rules at the left hand side and one or more stopping rules at the right hand side are accepted.
information about items that could be administered in the future \((N - k)\), in order to be able to assign examinees to a certain level. To avoid this potential problem, we calculated optimal descending ordering of Fisher item information at \(\hat{\theta}_k\) after every item administered. Table 2 represents the stopping rules as they are applied when \(k^* < k < N\). At \(k = N\), testing is stopped, and the decision rules from the TSPRT are applied.

Simulation studies

Three simulation studies were conducted. Two studies were conducted using only one cut point, and one study using two cut points. In all studies, the same generated data was used per experiment for both sequential rules. The simulations were programmed in the R software environment for statistical computing and graphics (R Development Core Team, 2008). In our simulations we used the more conservative \(\tilde{\theta}\) as an estimate for \(\theta\).

Figure 2. Simulation Study 1: Replication of Finkelmann(2003)

Simulation 1: Replication Study

The first study was conducted to replicate Finkelmann’s results (2003). The same distribution and number of item parameters were used, \(a_j \sim U[0.5, 1.5]\), \(b_j \sim U[-4, 4]\), and the item bank consisted of 300 items. The same cut point, maximum number of items, and values for gamma, alpha, and beta were used, \(N_{\text{max}} = 50\), \(\theta_0 = -0.325\), \(\gamma = 0.95\), \(\delta = 0.2\), \(\alpha = 0.05\), \(\beta = 0.05\). The only differences were the use of the WML-estimator (Warm, 1989; see Eq. 2) and the use of a slightly different version of the Fisher information function (see Eq. 3).

Fifteen equidistant theta values were used as ability parameters for the simulees, with 2000 replications per value. Figure 2 depicts the percentage of correctly classified simulees per theta value and the mean number of items used before a classification decision was taken.
Results. The percentage of correctly classified simulees was the same for both the TSPRT and the SCSPRT. The difference in mean number of items used between the SPRT and SCSPRT was quite large, with a minimum of 6.93 items and a maximum of 13.12 items near the cut point. This is a larger mean difference than Finkelman (2003) reported.

Simulation 2: Study with Real Item Parameters

The second study was conducted using real item parameters from the Eggen and Straetmans (2000) study. These item parameters originate from a mathematics item bank consisting of 250 calibrated items. To satisfy the necessary scaling constraints, the geometric mean of the estimated discrimination indices was fixed at $(\prod \hat{a}_j)^{1/250} = 3.10$, and the sum of the estimated difficulty parameters was fixed at $\sum_{j=1}^{N} \hat{b}_j = 0$. The cut points between the three classification levels, $\theta_1 = -0.13$ and $\theta_2 = 0.33$, were set as realistic values (see Eggen & Straetmans, 2000). However, because only one cut point was needed in this study, we used $\theta_2$ as the one cut point. The error rates were set at $\alpha_1 = \beta_1 = 0.05$, and the delta-regions at $\delta_{11} = \delta_{22} = 0.1$. The maximum number of items $N$ was set at $N_{max} = 40$. The value of $\gamma$ was set at $\gamma = 0.975$. The ability of every simulee $\theta_j$ was randomly drawn from a distribution with a mean of 0.294, and a standard deviation of 0.522; this was the ability distribution estimated in the calibration study. The point at which further measures of truncation could start was set at, following Finkelman (2003), $k^* = 20$. The number of simulees was set at 5000.

Results. The results showed that with a realistic cut point, ability distribution, realistic parameters, delta regions, and error rates, the percentage of correctly classified simulees was exactly the same for the SPRT and the SCSPRT: 95.05%. The mean difference between the number of items used by the SPRT and SCSPRT was 0.42 items, in favor of the SCSPRT. This is a much smaller difference than what was found in Study 1. Figure 3 shows the results for 10 equidistant theta points with 2000 replications per point. This figure shows that the
SCSPRT uses slightly fewer items than the SPRT, especially near the cut point, while maintaining virtually the same percentage of correctly classified simulees. An explanation for this relatively small observed difference (Finkelman, 2008) is that the SCSPRT works less efficiently when there are items administered with high discrimination ($a$-) parameters, with difficulty ($b$-) parameters around the cut point. In the mathematics item bank that was studied there are items, that are highly informative (high $I$) around the cut point, which might explain the smaller observed difference. To test this hypothesis, we reduced the mathematics item bank to the items with low discrimination ($a$-) parameters. The items with an $a$-parameter above three were omitted, resulting in an item bank consisting of 52 items with $a = 2$, and 115 items with $a = 3$ (167 items total). The result of this exploration was exactly as Finkelman (2008) predicted. With 2000 simulees, the difference between the TSPRT and SCSPRT in number of items used, before a classification decision was made, was 2.71 items. This is still a more modest result than with the theoretical item bank, but it is a substantial difference. The percentage of correctly classified simulees was 94.35% for the TSPRT and 94.45% for the SCSPRT.

![Figure 4. Simulation Study 3: Two cut points with realistic settings](image)

**Simulation 3: Study with 2 Cut Points**

**Item bank.** The same item bank, model configurations, and data simulation methods were used as in Study 2. The ability parameters were also randomly drawn from the same distribution. The difference in terms of data and item configuration was the use of an additional cut point, $\theta_1 = -0.13$ (see Eggen & Straetmans, 2000). In order to produce figures (see Figure 4) for the most efficient item selection method, ten equidistant theta values were used as ability parameters for the simulees, with 2000 replications per value.

**Item selection.** The most important difference was that with two cut points, it was not clear which item selection method would produce the best results. Therefore, three different item selection methods were explored: selection in the exact middle between the two cut
points, selection at the nearest cut point, and selection at the current theta estimate $\hat{\theta}_k$. Information on 'future' items was also chosen at these points. For the third method, this resulted in different 'future' items after every item administration.

**Table 3: Results of different item selection methods with the SPRT vs SCSPRT**

<table>
<thead>
<tr>
<th>Item selection method</th>
<th>SCSPRT % correct</th>
<th>SPRT % correct</th>
<th>SCSPRT N</th>
<th>SPRT N</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max $I$ in the middle</td>
<td>91.1</td>
<td>91.9</td>
<td>21.7</td>
<td>22.9</td>
</tr>
<tr>
<td>Max $I$ at nearest cut point</td>
<td>90.7</td>
<td>91.2</td>
<td>19.2</td>
<td>20.1</td>
</tr>
<tr>
<td>Max $I$ at current $\hat{\theta}$</td>
<td>90.9</td>
<td>91.3</td>
<td>19.3</td>
<td>19.7</td>
</tr>
</tbody>
</table>

**Results.** As can be seen in Table 3, the results of selection with maximum information at the nearest cut point and selection at the current theta estimate are similar. Results of item selection in the middle, between the two cut points, are somewhat worse. The preferred method here is selection with maximum information at the current theta estimate because this method is much more flexible regarding exposure control and content balancing methods. This means that this selection method is of much more practical use because a larger part of the item bank can be used. Figure 4 gives the mean number of items used per equidistant theta value and gives the mean percentage correct per theta value. This figure shows that the percentage of correctly classified simulees is similar for the SCSPRT and SPRT, but that the SCSPRT uses fewer items on average, especially near the cut points.
Discussion

One cut point

When using one cut point, the performance of the SCSPRT with a theoretical item bank is much more efficient than the SPRT. With a real item bank, under realistic circumstances, the gain in efficiency of the SCSPRT compared to the SPRT is more modest, but still quite substantial. Finkelman (2008) is correct in his conclusion that when highly discriminating items are omitted, the performance of the SCSPRT increases. However, our conclusion is that the results are highly item bank dependent because the results with realistic settings, even when highly discriminating items are omitted, are more modest compared to our results with the theoretical item bank.

Two cut points

A generalisation to more than two categories is possible. The performance of the SCSPRT with a real item bank is in general better than the SPRT with respect to the number of items needed for classification. This results in only a minimal loss in the percentage of correct classification decisions. For both the SCSPRT and SPRT, the selection method which chooses items with maximum information at the midpoint between the cutting points performs worse than the two other methods explored. As is the case with the SPRT, there are no big differences in performance between the remaining item selection methods; maximum information at the nearest cut point and maximum information at the current ability estimate are similar.

Future research

Additional results showed that if the cut points were set further apart, while keeping everything else the same, the efficiency gain became larger for the SCSPRT as opposed to the SPRT. This must be due to the effect observed by Finkelman (2008) that the gain is larger when there are only items with low discrimination parameters available in a certain proficiency area. However, different types of item banks should be explored to test the SCSPRT in different situations.
References


